Name: \_\_\_\_\_

MTH 150 Exam 4 May 8, 2007

**DIRECTIONS:** Calculators are permitted on this part of the exam. However, answers based solely on calculator results are unacceptable. You must still <u>show all</u> <u>work</u> to receive full credit. Good luck.

1. The region whose area is given by the definite integral  $\int_{1}^{2} (10 - x^3) dx$  is shown below.



(a) (6 points) Approximate the area of the above region using left endpoints of 4 subintervals (rectangles) of equal width.

(b) (4 points) Use the Fundamental Theorem of Calculus to find the <u>exact</u> area.

2. Evaluate the definite integrals. Decimal approximations from the calculator earn **no credit**.

(a) **(5 points)** 
$$\int_{-2}^{-1} \left( u - \frac{1}{u^2} \right) du$$

(b) (5 points) 
$$\int_{0}^{1} \frac{4}{1+x^2} dx$$

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**DIRECTIONS:** This is a <u>closed book</u>, <u>closed notes</u> exam. <u>No electronic devices</u> are allowed (this means calculators, computers, cell phones, pagers, etc.). Be neat and <u>show all work</u> to receive full credit. Correct answers without the supporting evidence to back it up (except where indicated) receive only partial credit. Good luck.

3. (5 points) Find an antiderivative of  $f(x) = \frac{1}{x} + 5x^2$ .

A.  $\ln |x| + \frac{5}{3}x^3$ B.  $-\frac{1}{x^2} + 10x$ C.  $\ln |x| + 10x$ D.  $-\frac{1}{x^2} + \frac{5}{3}x^3$ E. None of these

4. (5 points) Given that  $\int_{0}^{5} f(x) dx = 4$ , find the value of  $\int_{-2}^{3} f(x+2) dx$ .

| A. | 5 | D. 8 |  |
|----|---|------|--|
| B. | 4 | E. 3 |  |
| C. | 6 |      |  |

5. (**5 points**) Given a smooth, continuous function, which of the following statements is unconditionally true?

- A. Differentiability  $\Rightarrow$  Continuity  $\Rightarrow$  Integrability
- B. Integrability  $\Rightarrow$  Continuity  $\Rightarrow$  Differentiability
- C. Continuity  $\Rightarrow$  Integrability  $\Rightarrow$  Differentiability
- D. Differentiability  $\Rightarrow$  Integrability  $\Rightarrow$  Continuity
- E. None of these

6. (**5 points**) Which of the following integrals can NOT be evaluated using the Basic Integration Rules?

A.  $\int 5^x dx$ D.  $\int \sinh x dx$ B.  $\int \sec x dx$ E.  $\int \sec^2 x dx$ C.  $\int \ln x dx$ 

7. (5 points) Given 
$$\int_{0}^{3} f(x) dx = 4$$
 and  $\int_{3}^{6} f(x) dx = -1$ , evaluate  $\int_{0}^{6} \left[ f(x) + 2 \right] dx$ .  
A. 3 D. 12  
B. 5 E. 15  
C. 6

8. (**5 points**) Which of the following is a graphical representation of the Mean Value Theorem for Integrals?



9. (5 points) Find the particular solution of the differential equation  $f'(x) = \sin x$  given that  $f(\pi) = 2$ .

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      A. -\cos x + 1
      D. \cos x + 2

      B. \cos x + 3
      E. -\cos x + 3

      C. -\cos x
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10. (5 points) Find F'(x) given that  $F(x) = \int_{1}^{x^3} \sec t \, dt$ .

A.  $\sec(x^3)$ D.  $\sec^2(x^3)\tan(x^3)$ B.  $\sec^2(x^3)$ E. None of theseC.  $3x^2 \sec(x^3)$ 

11. (**10 points**)  $\int \sec(6x) dx$ 

12. (**10 points**)  $\int x\sqrt{x+2} \, dx$ 

13. (10 points) 
$$\int \frac{x+2}{\sqrt{4-x^2}} dx$$

14. (10 points) 
$$\int \frac{x^2 - 3x + 2}{x + 1} dx$$

## **BONUS (Optional 10 points)**

If *f* is a continuous function such that  $\int_{0}^{x} f(t) dt = xe^{2x} + \int_{0}^{x} e^{-t} f(t) dt$  for all *x*, find an explicit formula for f(x).